# Business cycles and the two margins of labor adjustment 

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## Introduction

- New Keynesian model with (or without) nominal and real rigidities is the reference framework for business cycle analysis.
- Model based on agents that are optimizing intertemporally that can be used for policy analysis.
- However, the standard version of the model (Woodford (2003), Gali (2008)) has no unemployment!
- Recent literature introduced labor market frictions in the New Keynesian model to study unemployment dynamics
- Frictions in the labor market because it is costly to find a match and it takes time (Mortensen-Pissarides).


## Introduction

(1) Real Business Cycle models. Seminal contributions by Andolfatto (1996) and Merz (1995). Fluctuations are driven only by neutral technology shocks.

- Shimer (2005 and 2009): the model does not deliver enough employment volatility.
(2) Monetary models with nominal and real rigidities: Walsh (2005), Trigari (2004 and 2006). Fluctuations are driven by monetary shocks. Challenge: explain inflation persistence
- Labor market frictions do not help generating more inflation persistence.
(3) Estimated models with a series of shocks using Bayesian techniques (Gertler, Sala and Trigari (2007), Groshenny (2009))
- The performance of the model is at best comparable with standard models with no labor market frictions (Smets-Wouters 2007)
- Large problems of identification. No internal propagation (Lubik 2009)


## Introduction

- Our paper also studies the role of labor market frictions in the transmission mechanism for shocks (technology, investment-specific and monetary).
- In particular, we consider the effects on the two margins of labor adjustment:
- Extensive margin (number of workers): fluctuations in employment
- Intensive margin (hours per capita): fluctuations in hours
(1) Review some empirical evidence on the adjustment along the two margins
(2) Provide a model that is able to deliver a reasonable split across the two margins
(3) Compare with existing literature


## Motivation: empirical evidence

- Unconditional evidence: In the data, around $1 / 3$ of the overall volatility of hours worked is due to variation in hours per worker (Krause and Lubik (2009)).

| Standard Deviation in US data |  |  |  |
| :---: | :---: | :---: | :---: |
| Unemployment | Hours per capita | Total hours | GDP |
| 7.71 | 0.30 | 1.10 | 1.41 |

- Motivation for having a model with two margins
- Fluctuations on the hours margin are not negligible but much larger volatility in employment.
- The second margin imposes more discipline on the theoretical model


## Motivation: empirical evidence

- Conditional evidence: Positive neutral technology shocks contract both hours and employment, but employment reacts slightly more. Canova, Lopez-Salido and Michelacci (2009)
- Similar results in Baleer (2007) and Barnichon (2008). Consistent with Gali (1999).
- Conditional evidence: Expansionary monetary policy shock expand both hours and employment but employment reacts more (Trigari, 2008).
- Conditional evidence: Positive investment-specific shocks expand hours per capita whereas the employment response is not significant. (Canova et al. 2009).


## Motivation: theory

- Krause and Lubik (2009): the RBC model with two margins of labor adjustment has difficulty explaining the relative volatilities of hours and employment
- hours per worker are too volatile relative to employment
- the model cannot explain the volatilities of vacancies and unemployment (Shimer puzzle).
- The same is true in New Keynesian models with nominal and real rigidities.


## Our contribution

Our goal is to provide a theoretical model that is able to obtain a reasonable split across the two margins. Important ingredients in our model:
(1) Timing assumption (as in Ravenna and Walsh (2008))
(2) Bargaining set-up (as in Sveen and Weinke (2007))

These two features are useful to increase the adjustment through the employment margin.

## The timing assumption

We follow Ravenna and Walsh (2008) and Blanchard and Gali (2009)

- Employment is not a predetermined variable (instantaneous hiring).

$$
\begin{equation*}
N_{t}(i)=(1-s) N_{t-1}(i)+L_{t}(i) . \tag{1}
\end{equation*}
$$

- In case of separation, workers can find a job in the period.


## The bargaining set-up

- Firms trade-off on the use of the two margins of labor adjustment:
- Using hours more intensively increases average wages
- Hiring new workers is costly (hiring cost)
- This is achieved by a specific bargaining set-up where the firm takes rationally into account that using hours more intensively increases average wages (Sveen and Weinke 2007)
- Wages are set by Nash bargaining
- Hours are decided by firms in a game where the firm is the leader and the wage negociation is the follower
- In the Right to Manage framework (Trigari 2006) the firm is the follower and takes the wage as given.


## Preview of the results

- Neutral technology shocks.
- The model implies a large response of employment and can reproduce the evidence for plausible calibrations.
- Nominal and real rigidities are essential.
- Investment-specific shocks
- The adjustment is achieved mainly through hours in keeping with the evidence
- Little propagation in the model for a plausible labor supply elasticity
- Monetary shocks
- The adjustment is achieved mainly through employment in keeping with the evidence and confirming results in Sveen and Weinke (2007).


## Our framework in perspective

- Our model relies on Ravenna and Walsh (2008) and Sveen and Weinke (2007)
- It includes capital accumulation (potentially important for technology shocks, Shimer 2009)
- It includes nominal and real rigidities (important for monetary shocks)
- it includes variable capacity utilization for completeness (third margin of adjustment).
- Few papers have two margins of labor adjustment and capital accumulation: Krause and Lubik (2009), Andolfatto (1996).


## Our framework in perspective

- Canova, Lopez-Salido and Michelacci (2009) rationalize their evidence in the context of a growth model featuring a vintage structure of technology shocks and search and matching frictions in the labor market.
- Trigari (2008) studies monetary shocks in a model with endogenous separation.
- We provide an alternative explanation using a model that is close to the "standard" New Keynesian model.


## Baseline Model

## Households

$$
\begin{gather*}
E_{t} \int_{0}^{1}\left[\sum_{k=0}^{\infty} \beta^{k} U\left(C_{t+k}, H_{t+k}(h)\right)\right] d h,  \tag{2}\\
U\left(C_{t}, H_{t}(h)\right)=\ln \left(C_{t}-h C_{t-1}\right)-\chi \frac{H_{t}(h)^{1+\eta}}{1+\eta},  \tag{3}\\
P_{t}\left(C_{t}+I_{t}+f\left(U T_{t}\right)\right)+D_{t} \leq \\
\quad D_{t-1} R_{t-1}+P_{t} W_{t} H_{t} N_{t}  \tag{4}\\
+B Z_{t} \Psi_{t}^{1+-\alpha} U_{t}+T_{t}+P_{t} R_{t}^{K} K_{t} .  \tag{5}\\
\bar{K}_{t+1}=(1-\delta) \bar{K}_{t}+\Psi_{t}\left(1-S\left(\frac{I_{t}}{I_{t-1}}\right)\right) I_{t},  \tag{6}\\
K_{t}=U T_{t} \bar{K}_{t}
\end{gather*}
$$

## Baseline Model

## Firms

- Technology is Cobb-Douglas

$$
\begin{equation*}
Y_{t}(i)=K_{t}(i)^{\alpha}\left(Z_{t} N_{t}(i) H_{t}(i)\right)^{1-\alpha} \tag{7}
\end{equation*}
$$

- We follow Blanchard and Galí (2007) in assuming restrictions on firms' hiring decisions.
- The law of motion of employment

$$
\begin{equation*}
N_{t}(i)=(1-s) N_{t-1}(i)+L_{t}(i) . \tag{8}
\end{equation*}
$$

- Hiring costs (per unit of employment)

$$
\begin{equation*}
G_{t}=\mathrm{Y} Z_{t} \Psi_{t}^{\frac{\alpha}{1-\alpha}}\left(\frac{L_{t}}{U_{t}^{S}}\right)^{\vartheta} \tag{9}
\end{equation*}
$$

where $U_{t}^{S} \equiv 1-(1-s) N_{t-1}$.

## Baseline Model

## Firms

- Each firm $i$ maximizes the following problem:

$$
\sum_{k=0}^{\infty} E_{t}\left\{\Lambda_{t, t+1}^{R}\left[\begin{array}{c}
Y_{t+k}(i) \frac{P_{t+k}(i)}{P_{t+k}}-R_{t+k}^{K} K_{t+k}(i) \\
-W_{t+k}(i) N_{t+k}(i) H_{t+k}(i)-G_{t+k} L_{t+k}(i)
\end{array}\right]\right\}
$$

s.t.

$$
\begin{aligned}
Y_{t+k}(i) & =\left(\frac{P_{t+k}(i)}{P_{t+k}}\right)^{-\epsilon} Y_{t+k} \\
Y_{t+k}(i) & =K_{t+k}(i)^{\alpha}\left(Z_{t+k} N_{t+k}(i) H_{t+k}(i)\right)^{1-\alpha}, \\
N_{t+k}(i) & =(1-s) N_{t+k-1}(i)+L_{t+k}(i), \\
P_{t+k+1}(i) & = \begin{cases}P_{t+k+1}^{*}(i) & \text { with prob. }(1-\theta) \\
P_{t+k}(i) & \text { with prob. } \theta\end{cases}
\end{aligned}
$$

## Baseline Model

## Firms

- The remaining first-order conditions read

$$
\begin{align*}
W_{t}(i)+\frac{\partial W_{t}(i)}{\partial H_{t}(i)} H_{t}(i)= & \frac{(1-\alpha) M C_{t} Y_{t}(i)}{H_{t}(i) N_{t}(i)}  \tag{10}\\
W_{t}(i) H_{t}(i)+G_{t}= & (1-\alpha) M C_{t} Y_{t}(i) / N_{t}(i) \\
& +(1-s) E_{t}\left\{\Lambda_{t, t+1}^{R} G_{t+1}\right\} \tag{11}
\end{align*}
$$

- The two equations have similar interpretations:
- On the LHS is the cost of increasing the use of hours or hiring an additional worker.
- On the RHS is the benefit of the marginal hour or worker.


## Baseline Model

## Wage Bargaining and Monetary Policy

- The wage resulting from the bargain is then

$$
\begin{equation*}
W_{t}(i) H_{t}(i)=\chi C_{t} \frac{H_{t}(i)^{1+\eta}}{1+\eta}+\Psi_{t} \tag{12}
\end{equation*}
$$

where

$$
\begin{align*}
\Psi_{t} \equiv & B Z_{t} \Psi_{t}^{\frac{\alpha}{1-\alpha}}+\frac{1-\phi}{\phi} G\left(F_{t}\right) \\
& -\frac{1-\phi}{\phi} E_{t}\left\{\Lambda_{t, t+1}^{R}(1-s)\left(1-F_{t+1}\right) G\left(F_{t+1}\right)\right\} \tag{13}
\end{align*}
$$

- Monetary policy rule

$$
\frac{R_{t}}{R}=\left(\frac{R_{t-1}}{R}\right)^{\rho_{R}}\left[\left(\frac{\Pi_{t}}{\Pi}\right)^{\phi_{\pi}}\right]^{1-\rho_{R}}
$$

where $\rho_{R}$ denotes the degree of interest rate smoothing.

## Baseline Model

## Calibration

$\eta=7$ (inverse of labor supply elasticity)
$\theta=0.66$ (price rigidity, slightly more than 3 quarters) $h=0.8$ (habit persistence)
$\phi=1 / 2$ (bargaining power)
$B=0.4$ (unemployment benefits)

| $\beta$ | $\chi$ | $\epsilon$ | $\delta$ | $\alpha$ | $\lambda_{1}$ | $\lambda_{2}$ | $\vartheta$ | $\phi_{\pi}$ | $\rho_{R}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.99 | $H=\frac{1}{3}$ | 7 | 0.025 | 0.33 | 0.33 | 1 | 1 | 1.5 | 0.9 |


| $U$ | $N=1-U$ | $F$ | $s=\frac{F * U}{(1-F) * N}$ | $U^{s}=1-(1-s) N$ |
| :---: | :---: | :---: | :---: | :---: |
| 0.057 | 0.943 | 0.71 | 0.148 | 0.197 |

## Results



## Results: Volatility

St.Dev. (relative to GDP)

|  | U | N | H | Tot. H |
| :---: | :---: | :---: | :---: | :---: |
| Data | 5.46 |  | 0.21 | 0.78 |
| Neutral | 3.85 | 0.22 | 0.17 | 0.39 |
| Inv.Spec. | 1.46 | 0.08 | 0.2 | 0.19 |
| Monetary | 7.58 | 0.45 | 0.23 | 0.69 |

- Monetary shocks produce large employment fluctuations, comparable to the unconditional data.
- Neutral technology shocks imply a fair amount of employment volatility.
- Investment-specific shocks barely affect the labor market.


## Results: neutral technology shocks



## Results: neutral technology shocks

- With flexible prices, no habits and no investment adjustment costs, the model is close to reproduce the Blanchard-Gali (2009) "neutrality result", although capital accumulation is modeled explicitly.
- With nominal and real rigidities the model achieves an equal split on the two margins and rationalizes the evidence by Canova et al. (2009).
- When $\eta>7$ the employment response is larger.


## Results: investment-specific shocks



## Results: investment-specific shocks

- Employment almost does not move in keeping with the evidence.
- Hours move more but still very little propagation.
- Nominal and real rigidities barely affect the transmission mechanism


## Results: monetary shocks



Adjustment is larger on the employment margin as in Sveen and Weinke (2007)

## Results: sensitivity to labor supply elasticity



## Results: sensitivity to labor supply elasticity



## Results: sensitivity to labor supply elasticity

- Several papers (Jaimovich and Rebelo (2009), Ravn and Simonelli (2008), Schmitt-Grohe and Uribe (2008)) study investment-specific shocks
- Large propagation
- Positive comovement between consumption and investment
- All these papers use $\eta$ around 0.4 arguing that it refers to variations across both margins.
- Here we model explicitly the two margins but we still need $\eta$ around 0.4 to obtain propagation.
- No propagation and the impact consumption response is at most zero for plausible values of $\eta$ (see Furlanetto, Gomes and Seneca (2009)).


## Conclusion

- We present a New Keynesian model that obtains a reasonable split across the two margins of labor adjustment
- Large employment variations in response to technology shocks and monetary shocks.
- Relatively larger response of hours in response to investment shocks. However, no propagation.
- The use of a very elastic labor supply in models with one margin is not justified.


## Baseline Model

## Wage Bargaining

- The household's value of a match with firm $i$

$$
\begin{align*}
\widetilde{W}_{t}(i)= & W_{t}(i) H_{t}(i)-\chi_{t} C_{t} \frac{H_{t}(i)^{1+\eta}}{1+\eta} \\
& +E_{t}\left\{\Lambda _ { t , t + 1 } ^ { R } \left[(1-s) \widetilde{W}_{t+1}(i)\right.\right. \\
& \left.\left.+s\left(F_{t+1} \widetilde{W}_{t+1}+\left(1-F_{t+1}\right) \widetilde{U}_{t+1}\right)\right]\right\} \tag{14}
\end{align*}
$$

where $\widetilde{W}_{t} \equiv \int_{0}^{1} \widetilde{W}_{t}(i) \frac{L_{t}(i)}{L_{t}} d i$ and $F_{t} \equiv \frac{L_{t}}{U_{t}}$.

- The value of being unemployed

$$
\begin{equation*}
\widetilde{U}_{t}=B Z_{t} \Psi_{t}^{\frac{\alpha}{1-\alpha}}+E_{t}\left\{\Lambda_{t, t+1}^{R}\left[F_{t+1} \widetilde{W}_{t+1}+\left(1-F_{t+1}\right) \widetilde{U}_{t+1}\right]\right\} \tag{15}
\end{equation*}
$$

## Baseline Model

## Wage Bargaining

- As in Blanchard and Galí (2009) the value of a match for firm $i$ corresponds to the cost of hiring a worker

$$
\begin{equation*}
\widetilde{J}_{t}(i)=G\left(F_{t}\right), \tag{16}
\end{equation*}
$$

which is independent of the firm.

- Surplus splitting implies

$$
\begin{equation*}
(1-\phi) \widetilde{J}_{t}=\phi\left(\widetilde{W}_{t}(i)-\widetilde{U}_{t}\right) \tag{17}
\end{equation*}
$$

where $(1-\phi)$ denotes the weight of workers in the bargain.

